Letter

Light beam induced finger instability in a photosensitive liquid crystal cell

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Interfaces limiting two phases in driven systems may exhibit rich dynamical behaviors. Optically induced phase transitions are of particular interest for the study of interfacial phenomena. Dye-doped liquid crystals offer an ideal scenario in which phase transitions can be induced by purely optical means. Light-driven interface dynamics and spatial structure have been partially unveiled. Here we report the emergence of fingerlike structures at the nematic-isotropic interface in a photoisomerization experiment. A reduced model reveals the instability origin, which is derived from a model for the dopant concentration and the order parameter. Analogously to the hydrodynamically triggered finger instability, the interdigital space follows a power law. When the cell is in the isotropic phase and the light turns off, transient foamlike and labyrinthine textures are observed. Numerical simulations reproduce the observed behaviors. Our findings open an avenue for optically addressed interfacial dynamics and shape tailoring of spatial textures, not only liquid crystals but also polymers.

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Interfaces are the physical borderline between two immiscible phases of matter. Depending on the nature of the states connected, interfaces can undergo spatial instabilities, exhibiting complex dynamical behaviors and displaying enthralling shapes. Interfacial phenomena can be found in multiple physical systems and have been a subject of study for decades. A paradigmatic example that has accompanied and intrigued humanity since its dawn is the spread of fire [1,2]. The interface instability is the result of an unbalance between expansive and limiting factors. Snowflake growth is perhaps the most famous case of interface instability leading to intriguing motifs due to heat diffusion limitations [3]. Interfacial instabilities have also been observed in metal deposition [4], where the limitation is the electrodiffusion; retinal vessel growth [5]; and bacterial colonies [6], where mass diffusion is the limiting factor. One of the most studied scenarios is viscous fingering, also known as finger instability, where fingerlike structures grow when a low-viscosity fluid is injected into a higher one, creating paths of lower resistance [7,8]. The fingering phenomenon was initially studied in molasses-water mixtures [9] and later studied in a more controllable setup in which a fluid is in a Hele-Shaw cell while another immiscible fluid is injected [10]. Finger instabilities can be found in other contexts, such as in elastic buckling [11] and laser-induced implosions in cylindrical tubes [12]. All cited interfacial instabilities are spontaneously emergent or controlled by hydrodynamic injection, thermal, or electro-osmotic pressure [13].

In recent years, liquid crystal based optical systems have been shown to be of great interest for the study and tailoring of complex interfacial phenomena because of their high control due to light beam shaping techniques [14,15]. Liquid crystals are a state of matter that is allowed to flow like conventional liquids while having properties usually attributed to solids like birefringence and can exist in a multitude of phases with varying degrees of order [16,17]. Depending on the mechanism used to trigger the phase transitions between the mesophases, liquid crystals are classified as thermotropic, lyotropic, or polymeric, among others [18]. For optical applications, it is desired to control either the material's physical properties or its light response. By incorporating a photoresponsive dopant (typically, an azo dye), the coupling between the liquid crystal and light can be amplified [17,19,20]. Upon illumination, the azo dye undergoes a photoisomerization process, inducing a phototropic host-guest phase where the nematic liquid crystal changes to an isotropic state [21,22]. This phenomenon is known as the Jánossy effect. The nematic-isotropic optically induced phase transition is of particular interest for birefringence control. This opens the possibility of optically operated devices [23–25]. Since the discovery of the Jánossy effect, most advances have focused on creating new mixtures by improving the azo dye molecules' response and

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characterizing their linear and nonlinear responses. Lightdriven interface dynamics between coexisting mesophases have remained concealed except for some simple configurations. Propagation of locally flat nematic-isotropic interfaces has been observed in cells with planar anchoring [15] and soliton propagation in dye-doped liquid crystal cells [26]. Recently, the emergence of patterns in dye-doped liquid crystal cells due to differences between the *cis*-isomer diffusion and molecular orientation timescales [27–29] and light-induced motion of dye-doped liquid crystal droplets [30–34] was reported.

This Letter aims to describe the emergence of light-induced fingering instability of a nematic-isotropic interface in a liquid crystal photoisomerization experiment while having the possibility of controlling propagation speed, finger length, and average interdigital spacing by optical means. Furthermore, the system shows complex foamlike and labyrinthine textures when the process is reversed by decreasing the light intensity. We propose a phase-field model that reproduces all the observed behaviors based on reaction-diffusion equations for the liquid crystal order parameter and the *cis*-state dye concentration. These results open the avenue for developing new optical techniques for controlling liquid crystal and polymeric mixtures textures.

The experimental setup is depicted in Fig. 1(a). We used a dye-doped liquid crystal cell (DDLCC) consisting of a nematic liquid crystal mixed with methyl red dye and sandwiched between two polyvinyl alcohol-coated glass plates separated by 25 μ m thanks to boundary spacers. The liquid crystal is commercially available E7 (by Instec), with elastic constants $K_1 = 11.2$, $K_2 = 6.8$, and $K_3 = 18.6$ (×10⁻¹² N) and dielectric constants $\epsilon_{\parallel} = 18.96$ and $\epsilon_{\perp} = 5.16$. The dye corresponds to a methyl red dye (2-N, N-dimethyl-4aminophenyl) which is mixed at a concentration of 0.5 wt % as solid crystal powder with the E7 liquid crystal. The mixture is heated to enhance mixing and homogenization of the mixture. The low concentration of dye ensures that the resulting material is a liquid crystal at room temperature and elastic property preservation while increasing the optical coupling. Once the mixture is homogeneous, it is injected between two polyvinyl alcohol coated glasses separated by $25 \,\mu m$ boundary spacers and rubbed to favor planar alignment and orthogonal to each other to create a planar twisted alignment cell [35]. The surface area of the cell is about 4 cm². This configuration favors the dopant molecules arranging in different orientations following the liquid crystal molecular orientation in the nematic phase, ensuring the necessary coupling with the light crossing the sample. A DDLCC region is illuminated with a Gaussian light beam from a frequency-doubled Nd⁺³:YVO₄ laser with a wavelength of 532 nm. The wavelength was selected to be in the absorption band of the methyl red dye [36]. Light absorption of the DDLCC has been measured which increases the sample temperature up to 38 °C under similar experimental conditions, 22 °C below the thermotropic nematic-isotropic transition [14]. Hence, under these thermal conditions, the system is in its nematic mesophase. The laser is expanded and spatially filtered using a Kepler telescope with a magnification of $5 \times$ and a pinhole placed in the focal point of the telescope. A double Glan Calcite polarizer is used to ensure the polarization of the beam. A single Glan Calcite polarizer or extinction



FIG. 1. Experimental setup and interface dynamics. (a) The system is irradiated by a frequency-doubled Nd⁺³:YVO₄ 532 nm green laser. A pair of lenses (BE) is used to expand the laser beam. A polarizer P is placed to add extra laser power control. The dye-doped liquid crystal cell (DDLCC) is placed after the first polarizer Pfollowing the beam propagation direction. The DDLCC has twisted anchoring. An analyzer A is placed to sample the birefringence of the DDLCC. The horizontal and entering the plane arrows indicate the polarization directions of the electric field, polarizer, anchoring, and analyzer. Namely, the polarizer P and analyzer A are oriented on the x and y axes, respectively. Imaging lenses (IL) and a CCD camera are used to acquire the images. (b) Schematic representation of the host-guest phototropic phase transition in the DDLCC. The Gaussian beam profile induces a spatial distribution of the photoisomerization rate in the guest dye methyl red, producing a decrease in the host liquid crystal nematic order. (c) Snapshots of the dye-doped liquid crystal textures obtained for different conditions. The left snapshot is obtained for green laser irradiation of 700 mW when the fingers reach their maximum extension, the central snapshot is for 10 mW irradiation starting from an isotropic bubble, and the right snapshot is an isotropic stationary bubble for irradiation of 700 mW.

polarizers can be used instead. The DDLCC cell with planar twisted anchoring is placed perpendicular to the optical axis. An analyzer crossed polarizer is placed to filter the light that passes through the liquid crystal cell. The analyzer corresponds to a Glan Calcite polarizer. A Kepler telescope with a magnification of $0.25 \times$ is used to record the light with a monochrome CCD camera with 1024×768 resolution recording at 20 frames per second. The DDLCC was subjected to input powers from 300 up to 700 mW. All experimental observations were made at room temperature. When the cell is not illuminated, the sample is in a homogeneous twisted nematic configuration, and the methyl red is in the trans isomer state, which tends to align with the orientational order of the liquid crystal molecules [37]. When illuminating, the methyl red undergoes isomerization, changing from a trans-isomer to a *cis*-isomer due to photoexcited molecular torque [38] [see Fig. 1(b)]. *Cis*-isomer molecules induce local disorder on the liquid crystal because of its inability to align with the nematic director [17,27]. For high illumination intensity, the system undergoes a host-guest phototropic transition where the nematic phase locally changes to an isotropic liquid [39].



FIG. 2. Experimental features of the spatial transversal instability. (a) Temporal evolution of the mean radius of the isotropic region. (b) The dynamics can be divided into four stages: (I) nucleation, (II) expansion, (III) saturation, and (IV) steady state. (c) For different light intensities, different average interdigital spacing emerges. The interdigital spacing is measured as the distance between two fingers when the isotropic bubble reaches its maximum radius (the transition from region II to region III. A power law with measured critical exponent -3.27 is fitted.

The system displays rich, diverse dynamics, from which we have identified three main behaviors [see Fig. 1(c)]: finger instability, foamlike texture, and labyrinthine texture. We first describe the behavior of the system upon illumination. It can be divided into four stages: nucleation, expansion, saturation, and the steady state [see Fig. 2(a)]. First, the nematic-isotropic transition occurs through the nucleation of isotropic bubbles into the nematic liquid crystal close to the center of the illumination zone. These bubbles are created due to inhomogeneities in the cell, which trigger the photoisomerization front in several places. The bubbles coalesce rapidly to form a single isotropic expanding bubble that invades the nematic liquid crystal following the dynamics dictated by the Gaussian light beam. Once a single bubble of the isotropic state is formed, the interface turns unstable, developing a spatial modulation. Instabilities of a moving nematic-isotropic interface-driven were reported [40,41]. This modulation gives rise to fingerlike structures that grow towards the isotropic state: the fingertips propagate slower than their base until they reach a maximum length (see the temporal sequence in Fig. 2(b). The number of fingers depends on the light intensity. Indeed, the finger average interdigital spacing decreases following a power law as the light intensity increases, as shown in Fig. 2(c). Analogous behavior is also observed in the Saffman-Taylor experiment, where the finger periodicity decreases with the capillary number [42]. This decrease suggests that in our experiment, a similar mechanism takes place. Namely, the interface follows the least hydrodynamic resistance path between two immiscible fluids, which are the nematic and isotropic phases. Later, the interface stops at the position where both nematic and isotropic phases are equally favorable. This position corresponds to the Maxwell point [15]. Subsequently, fingers shrink until the interface becomes circular. At this point, no further dynamic is observed, and the front becomes motionless.

Coupling between liquid crystal order parameter S and the *cis*-state photoisomerizable molecule concentration c has been used previously to model host-guest phototropic transitions on dye-doped liquid crystal cells with planar and twisted anchoring [27,28]. Close to a Turing spatial instability the following phase-field reduced model can be derived for the order parameter in a DDLCC subjected to Gaussian irradiation [27],

$$\partial_t u = \eta(r) + u - u^3 + D(r)\tilde{\nabla}^2 u - \nabla^4 u, \qquad (1)$$

where *u* is related to the order parameter of the liquid crystal. Notice $u \approx 1$ ($u \approx -1$) accounts for the nematic (isotropic) phase. $\eta(r) = \alpha(C_0 + C_1 e^{-r^2/\omega^2})$ is an inhomogeneous bifurcation parameter modeling preference of the material to have a nematic (isotropic) phase for $\eta > 0$ ($\eta < 0$) [15,27]. The parameters C_0 and C_1 are determined by the light intensity [27]. Hence, the bifurcation parameter inherits the laser beam intensity structure, having a Gaussian profile with respect to the radial coordinate *r*. α is a constant parameter tuning the coupling between the order parameter and the light intensity. $\tilde{\nabla}^2$ is an anisotropic diffusion operator with respect to the radial and the angular coordinate θ which reads

$$\tilde{\nabla}^2 = \left(\frac{\partial^2}{\partial r^2} + \frac{1}{r}\frac{\partial}{\partial r} + \lambda \frac{1}{r^2}\frac{\partial^2}{\partial \theta^2}\right).$$
 (2)

D(r) is an inhomogeneous diffusion coefficient. When D < 0, a Turing instability takes place, triggering pattern formation. Pattern formation is seen only on the nematic state, not in the isotropic one, for which we introduced a spatial dependence

$$D = D_H + D_I \tanh\left(\frac{r - r_0}{p}\right),\tag{3}$$

which allows the control of the pattern formation zone. λ is an angular anisotropy, which controls the fingering instability. For $\lambda = 1$, we obtain the conventional Laplacian operator. The intrinsic anisotropy of the liquid crystal matrix and the Gaussian illumination is the origin of the anisotropy, which favors the *cis*-state concentration transport in the radial direction. Similar models have been used for the host-guest phototropic transition on dye-doped liquid crystal cells with planar anchoring cells [14,15] and the emergence of stripe patterns in a cell with twisted anchoring [28]. The partial differential equation (1) is solved using a finite difference scheme



FIG. 3. Numerical simulations of equation Eq. (1). (a) Temporal sequence of the evolution of the order parameter *u* showing finger instability (black stands for $u \approx 0$) for $C_0 = -0.25$, $C_1 = 1.0$, $\omega = 58$, $D_H = -0.6$, $D_I = 1.9$, $r_0 = 105$, p = 40, and $\lambda = 1.5$ in a two-dimensional grid with 300 × 300 points. (b) Phase diagram in the parameter space { C_1 , λ } with the same values of the rest of the parameters as in (a). Regions I, II, and III account for concentric ring propagation, finger instability, and circular isotropic droplet propagation, respectively. (c) Typical experimental snapshots of the related phenomena for regions I, II, and III in the phase diagram.

in space that uses a centered stencil of seven grid points, where spatial derivatives are calculated using expansion up to order 4 in the reticle size. Time integration is performed using the Runge-Kutta algorithm with leading order 4. Figure 3(a) shows a temporal sequence of a typical simulation in which a nematic-isotropic interface develops a fingering instability as it propagates starting from a purely nematic initial condition. Varying parameters C_1 and λ , three different scenarios can be identified: concentric rings propagation, finger instability, and stable circular propagation. All these behaviors were observed in experiments.

Once the dye-doped liquid crystal is in the isotropic phase, the irradiation can be turned off, causing the nematic phase to invade the isotropic state. Surprisingly, the nematic to isotropic transition follows an entirely different course from the one described previously. The inverse process is characterized by the emergence of a foamlike texture of nematic bubbles as observed in Fig. 4(a). Subsequently, the bubbles start a coalescence process while shrinking, leading at the end to a labyrinthine texture that can remain for several minutes. Interestingly, Eq. (1) displays a similar dynamics when the parameter C_1 is abruptly decreased starting from a steady circular front [see Fig. 4(b)].

In brief, we have shown that light can induce finger instability in a liquid crystal photoisomerization experiment, leading to complex nematic-isotropic textures when the process is reversed. A simple phase-field model based on two reactiondiffusion equations for the order parameter and the *cis*-isomer of the azo dye reproduces all the observed behaviors. The



FIG. 4. Interface dynamics retraction for decreasing light intensity. (a) Temporal experimental snapshot sequence for the retraction of the isotropic phase when light intensity is decreased from $I_{\text{start}} =$ 0.7 W to $I_{\text{final}} = 0.05$ W. The snapshot t_2 corresponds to a foamlike texture, while t_3 is a labyrinthine texture. (b) Temporal sequence of the evolution of u, considering Eq. (1) starting from an isotropic bubble, in which the C_1 parameter is abruptly decreased. The values of the parameters are $C_0 = -1.0$, $C_1 = 0.3$, $\omega = 115$, $D_H = -2.4$, $D_I = 0.0$, and $\lambda = 0.2$, and a two-dimensional grid with 600 × 600 points was chosen.

control over the fingers' average interdigital spacing allows for the possibility to light-steered fingering instabilities and for interface roughness control. Finally, we foresee these possibilities not only in the reversible photoisomerization process as shown in the experiments but also in permanent photoisomerizable polymerizations, where controlling the growth interface could lead to different textures of the final polymeric product.

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