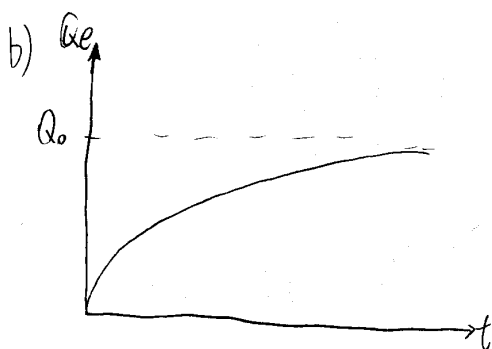


P2) a) Continuidad: $\frac{dV}{dt} = Q_a - Q_e$; $Q_a = Q_0$; $Q_e = \alpha \cdot h$; $V = A \cdot h$; pero $h = h(t)$

$$\Rightarrow A \cdot \frac{dh}{dt} = Q_0 - \alpha h \Leftrightarrow \frac{dh}{Q_0 - \alpha h} = \frac{1}{A} \cdot dt \Leftrightarrow \int_0^h \frac{dh}{Q_0 - \alpha h} = \frac{1}{A} \int_0^t dt$$

$$\Leftrightarrow \frac{-1}{\alpha} \cdot \ln(Q_0 - \alpha h) \Big|_0^h = \frac{1}{A} \Big|_0^t \Leftrightarrow \frac{-1}{\alpha} \ln\left(\frac{Q_0 - \alpha h}{Q_0}\right) = \frac{t}{A} \Leftrightarrow \ln\left(\frac{Q_0}{Q_0 - \alpha h}\right) = \frac{t \alpha}{A}$$

$$Q_0 = (Q_0 - \alpha h) \cdot e^{\frac{\alpha t}{A}} \Leftrightarrow Q_0 e^{-\frac{\alpha t}{A}} = Q_0 - \alpha h \Leftrightarrow h(t) = \frac{Q_0}{\alpha} (1 - e^{-\frac{\alpha t}{A}})$$



c) $Q_e = \alpha \cdot h = \alpha \frac{Q_0}{\alpha} (1 - e^{-\frac{\alpha t}{A}})$; $Q_e = 0.99 Q_0 = Q_0 (1 - e^{-\frac{\alpha t}{A}}) \Leftrightarrow 0.99 = 1 - e^{-\frac{\alpha t}{A}}$
 $e^{-\frac{\alpha t}{A}} = 1 - 0.99 \Leftrightarrow -\frac{\alpha t}{A} = \ln(0.01) \Leftrightarrow t = \frac{-A}{\alpha} \cdot -4.61 = \frac{4.61 A}{\alpha}$

Notar que cuando $t \rightarrow \infty \Rightarrow Q_e \rightarrow Q_0 (1 - e^{-\frac{\alpha t}{A}})_{t \rightarrow \infty} = Q_0$