

PI) $V(z) = 5 \cdot 10^6 \cdot e^{0,0558(z-20)}; t_e = 60$

$$Q_a = 156 + \frac{(406-156)}{86.400} t = 156 + 0,0029 t; (0 \leq t \leq 1 dia = 86.400 [s])$$

$$Q_a = 406 - \frac{(406-156)}{2 \cdot 86.400} t = 406 - 0,00145 t; (86.400 \leq t \leq 259.200 [s])$$

Continuidad: $\frac{dV}{dt} = Q_a - Q_e \xrightarrow{0} \Leftrightarrow \frac{dV}{dt} = Q_a \Leftrightarrow \int_{V_0}^{V_t} dV = \int_0^t Q_a dt$

a) $\int_{V(z=56)}^{V(z=60)} dV = \int_0^t (156 + 0,0029 t) dt \Leftrightarrow 5 \cdot 10^6 \cdot e^{0,0558 \cdot 40} - 5 \cdot 10^6 \cdot e^{0,0558 \cdot 36} = 156t + \frac{0,0029 t^2}{2}$

$$9.320.588 = 156t + 0,0029 t^2 \Rightarrow t = 42.756 [s]$$

b) $5 \cdot 10^6 \cdot e^{0,0558 \cdot 40} - 5 \cdot 10^6 \cdot e^{0,0558 \cdot 25} = 26.417.549 = 156t + \frac{0,0029 t^2}{2} \Rightarrow t = 91.508 [s] > 86.400$

$\Rightarrow$ Hay que usar ambas expresiones de caudal efluente

$$26.417.549 = \int_0^{86.400} (156 + 0,0029 t) dt + \int_{86.400}^t (406 - 0,00145 t) dt = 156t + \frac{0,0029 t^2}{2} \Big|_0^{86.400} + 406t - \frac{0,00145 t^2}{2} \Big|_{86.400}^t$$

$$\Leftrightarrow 26.417.549 = 156 \cdot 86.400 + \frac{0,0029 \cdot 86.400^2}{2} + 406t - \frac{0,00145 t^2}{2} \Rightarrow t = 177.575 [s]$$