



$$B_1 = Z_1 + \frac{P_1}{\rho g} + \frac{V_1^2}{2g} = -5$$

$$B_2 = B_1 - J_{1-2} + \Delta B = -5 - f \frac{(L_1 + S)}{D} \frac{V_{1-2}^2}{2g} + \Delta B \quad \text{con } V_{1-2} = \frac{(Q_A + Q_B)}{\frac{\pi D^2}{4}}$$

$$\Rightarrow B_2 = -5 + \Delta B - f \frac{(L_1 + S) \cdot 16 (Q_A + Q_B)^2}{\pi^2 D^5 2g}$$

$$B_A + B_2 - J_{2-A} = B_2 - f \frac{L_2}{D} \frac{V_{2-A}^2}{2g} \quad \text{con } V_{2-A} = \frac{Q_A}{\frac{\pi D^2}{4}}$$

$$B_A = -5 + \Delta B - f \frac{(L_1 + S) \cdot 16 (Q_A + Q_B)^2}{\pi^2 D^5 2g} - f \frac{L_2 \cdot 16 Q_A^2}{\pi^2 D^5 2g} = -5 + \Delta B - \frac{16 f}{\pi^2 D^5 2g} [(L_1 + S)(Q_A + Q_B)^2 + L_2 Q_A^2]$$

En el otro lado:

$$B_A = \cancel{Z_A + \frac{P_A}{\rho g} + \frac{V_A^2}{2g}} = \frac{16 Q_A^2}{\pi^2 D^5 2g}$$

$$\Rightarrow -5 + \Delta B - \frac{16 f}{\pi^2 D^5 2g} [(L_1 + S)(Q_A + Q_B)^2 + L_2 Q_A^2] = \frac{16 Q_A^2}{\pi^2 D^5 2g}$$

$$\Rightarrow -5 + \Delta B = \frac{16 f}{\pi^2 D^5 2g} \left[Q_A^2 \frac{D}{f} + (L_1 + S)(Q_A + Q_B)^2 + L_2 Q_A^2 \right] \quad (1)$$

Análogamente:

$$B_B = B_2 - J_{2-B} = B_2 - f \frac{L_2}{D} \frac{V_{2-B}^2}{2g} \quad \text{con } V_{2-B} = \frac{Q_B}{\frac{\pi D^2}{4}}$$

$$B_B = -5 + \Delta B - f \frac{(L_1 + S) \cdot 16 (Q_A + Q_B)^2}{\pi^2 D^5 2g} - f \frac{L_3 \cdot 16 Q_B^2}{\pi^2 D^5 2g} = -5 + \Delta B - \frac{16 f}{\pi^2 D^5 2g} [(L_1 + S)(Q_A + Q_B)^2 + L_3 Q_B^2]$$

En otro lado:

$$B_B = Z_B + \frac{P_B}{\gamma} + \frac{V_B^2}{2g} = 10 + \frac{16 Q_B^2}{T^2 D^2 2g}$$

$$\Rightarrow -S + \Delta B - \frac{16 f}{T^2 D^2 2g} [(L_1 + S)(Q_A + Q_B)^2 + L_2 Q_B^2] = 10 + \frac{16 Q_B^2}{T^2 D^2 2g}$$

$$\underline{-S + \Delta B = \frac{16 f}{T^2 D^2 2g} \left[Q_B^2 \frac{2}{f} + (L_1 + S)(Q_A + Q_B)^2 + L_2 Q_B^2 \right]} \quad (2)$$

Restando (1) con (2), tenemos:

$$10 = \frac{16 f}{T^2 D^2 2g} \left[Q_A^2 \left(\frac{D}{f} + L_2 \right) - Q_B^2 \left(\frac{D}{f} + L_2 \right) \right] \quad (3)$$

Si suponemos que Q_B es menor que $Q_A \Rightarrow Q_B = 1 \text{ l/s}$

Reemplazamos $Q_B = 1 \text{ l/s}$ en (3) se obtiene $Q_A = 5 \text{ l/s}$.

$$\Rightarrow Q_A = 5 \text{ l/s}$$

$$Q_B = 1 \text{ l/s}$$

Juego reemplazando Q_A y Q_B en (1) o en (2), se obtiene:

$$\Rightarrow \boxed{\Delta B = 22 \text{ m}}$$

∴ la bomba debe provocar una variación de Bernoulli de 22 m para que el caudal mínimo en A y B sea de 1 l/s.